## Time Synchronization and Logical Clocks

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CS 240: Computing Systems and Concurrency Lecture 5

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## Today

## 1. The need for time synchronization

2. "Wall clock time" synchronization
3. Logical Time

## A distributed edit-compile workflow



- $2143<2144 \rightarrow$ make doesn’t call compiler

Lack of time synchronization result a possible object file mismatch

## What makes time synchronization hard?

1. Quartz oscillator sensitive to temperature, age, vibration, radiation

- Accuracy ca. one part per million (one second of clock drift over 12 days)

2. The internet is:

- Asynchronous:" arbitrary message delays
- Best-effort: messages don't always arrive


## Today

## 1. The need for time synchronization

2. "Wall clock time" synchronization

- Cristian's algorithm, Berkeley algorithm, NTP

3. Logical Time

- Lamport clocks
- Vector clocks


## Just use Coordinated Universal Time?

- UTC is broadcast from radio stations on land and satellite (e.g., the Global Positioning System)
- Computers with receivers can synchronize their clocks with these timing signals
- Signals from land-based stations are accurate to about $0.1-10$ milliseconds
- Signals from GPS are accurate to about one microsecond
- Why can't we put GPS receivers on all our computers?


## Synchronization to a time server

- Suppose a server with an accurate clock (e.g., GPSdisciplined crystal oscillator)
- Could simply issue an RPC to obtain the time:

- But this doesn't account for network latency
- Message delays will have outdated server's answer


## Cristian's algorithm: Outline

1. Client sends a request packet, timestamped with its local clock $T_{1}$
2. Server timestamps its receipt of the request $T_{2}$ with its local clock
3. Server sends a response packet with its local clock $T_{3}$ and $T_{2}$
4. Client locally timestamps its receipt of the server's response $T_{4}$


Time $\downarrow$ synchronize its local clock to the server's local clock?

## Cristian's algorithm: Offset sample calculation

## Goal: Client sets clock $\leftarrow T_{3}+\delta_{\text {resp }}$

- Client samples round trip time $\delta=$ $\delta_{\text {req }}+\delta_{\text {resp }}=\left(T_{4}-T_{1}\right)-\left(T_{3}-T_{2}\right)$
- But client knows $\delta$, not $\delta_{\text {resp }}$

Assume: $\delta_{\text {req }} \approx \delta_{\text {resp }}$

Client sets clock $\leftarrow T_{3}+1 / 2 \delta$


Time $\downarrow$

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## Berkeley algorithm

- A single time server can fail, blocking timekeeping
- The Berkeley algorithm is a distributed algorithm for timekeeping
- Assumes all machines have equally-accurate local clocks
- Obtains average from participating computers and synchronizes clocks to that average


## Berkeley algorithm

- Master machine: polls L other machines using Cristian's algorithm $\rightarrow\left\{\theta_{i}\right\}(i=1 \ldots L)$

Master

(a)

(b)

(c)

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## The Network Time Protocol (NTP)

- Enables clients to be accurately synchronized to UTC despite message delays
- Provides reliable service
- Survives lengthy losses of connectivity
- Communicates over redundant network paths
- Provides an accurate service
- Unlike the Berkeley algorithm, leverages heterogeneous accuracy in clocks


## NTP: System structure

- Servers and time sources are arranged in layers (strata)
- Stratum 0: High-precision time sources themselves
- e.g., atomic clocks, shortwave radio time receivers
- Stratum 1: NTP servers directly connected to Stratum 0
- Stratum 2: NTP servers that synchronize with Stratum 1
- Stratum 2 servers are clients of Stratum 1 servers
- Stratum 3: NTP servers that synchronize with Stratum 2
- Stratum 3 servers are clients of Stratum 2 servers
- Users' computers synchronize with Stratum 3 servers


## NTP operation: Server selection

- Messages between an NTP client and server are exchanged in pairs: request and response
- Use Cristian's algorithm
- For $i^{\text {th }}$ message exchange with a particular server, calculate:

1. Clock offset $\theta_{i}$ from client to server
2. Round trip time $\delta_{i}$ between client and server

- Over last eight exchanges with server $k$, the client computes its dispersion $\sigma_{k}=\max _{i} \delta_{i}-\min _{i} \delta_{i}$
- Client uses the server with minimum dispersion


## NTP operation : Clock offset calculation

- Client tracks minimum round trip time and associated offset over the last eight message exchanges ( $\delta_{0}, \theta_{0}$ )
$-\theta_{0}$ is the best estimate of offset: client adjusts its clock by $\theta_{0}$ to synchronize to server



## NTP operation: How to change time

- Can't just change time: Don't want time to run backwards
- Recall the make example
- Instead, change the update rate for the clock
- Changes time in a more gradual fashion
- Prevents inconsistent local timestamps


## Clock synchronization: Take-away points

- Clocks on different systems will always behave differently
- Disagreement between machines can result in undesirable behavior
- NTP, Berkeley clock synchronization
- Rely on timestamps to estimate network delays
- 100s $\mu \mathrm{s}$-ms accuracy
- Clocks never exactly synchronized
- Often inadequate for distributed systems
- Often need to reason about the order of events
- Might need precision on the order of ns


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## Motivation: Multi-site database replication

- A New York-based bank wants to make its transaction ledger database resilient to whole-site failures
- Replicate the database, keep one copy in sf, one in nyc



## The consequences of concurrent updates

- Replicate the database, keep one copy in sf, one in nyc
- Client sends query to the nearest copy
- Client sends update to both copies



## Idea: Logical clocks

- Landmark 1978 paper by Leslie Lamport
- Insight: only the events themselves matter


Idea: Disregard the precise clock time Instead, capture just a "happens before" relationship between a pair of events

## Defining "happens-before"

- Consider three processes: P1, P2, and P3
- Notation: Event $\mathbf{a}$ happens before event $\mathbf{b}(\mathbf{a} \rightarrow \mathbf{b})$


Physical time $\downarrow$

## Defining "happens-before"

1. Can observe event order at a single process


Physical time $\downarrow$

## Defining "happens-before"

1. If same process and $\mathbf{a}$ occurs before $\mathbf{b}$, then $\mathbf{a} \rightarrow \mathbf{b}$


Physical time $\downarrow$

## Defining "happens-before"

1. If same process and $\mathbf{a}$ occurs before $\mathbf{b}$, then $\mathbf{a} \rightarrow \mathbf{b}$
2. Can observe ordering when processes communicate


Physical time $\downarrow$

## Defining "happens-before"

1. If same process and $\mathbf{a}$ occurs before $\mathbf{b}$, then $\mathbf{a} \rightarrow \mathbf{b}$
2. If $\mathbf{c}$ is a message receipt of $\mathbf{b}$, then $\mathbf{b} \rightarrow \mathbf{c}$


Physical time $\downarrow$

## Defining "happens-before"

1. If same process and $\mathbf{a}$ occurs before $\mathbf{b}$, then $\mathbf{a} \rightarrow \mathbf{b}$
2. If $\mathbf{c}$ is a message receipt of $\mathbf{b}$, then $\mathbf{b} \rightarrow \mathbf{c}$
3. Can observe ordering transitively


Physical time $\downarrow$

## Defining "happens-before"

1. If same process and $\mathbf{a}$ occurs before $\mathbf{b}$, then $\mathbf{a} \rightarrow \mathbf{b}$
2. If $\mathbf{c}$ is a message receipt of $\mathbf{b}$, then $\mathbf{b} \rightarrow \mathbf{c}$
3. If $\mathbf{a} \rightarrow \mathbf{b}$ and $\mathbf{b} \rightarrow \mathbf{c}$, then $\mathbf{a} \rightarrow \mathbf{c}$


Physical time $\downarrow$

## Concurrent events

- Not all events are related by $\rightarrow$
- a, d not related by $\rightarrow$ so concurrent, written as a || d


Physical time $\downarrow$

## Lamport clocks: Objective

- We seek a clock time C(a) for every event a

Plan: Tag events with clock times; use clock times to make distributed system correct

- Clock condition: If $\mathbf{a} \rightarrow \mathbf{b}$, then $C(\mathbf{a})<C(\mathbf{b})$


## The Lamport Clock algorithm

- Each process $\mathrm{P}_{\boldsymbol{i}}$ maintains a local clock $\boldsymbol{C}_{\boldsymbol{i}}$

1. Before executing an event, $\boldsymbol{C}_{\boldsymbol{i}} \leftarrow \boldsymbol{C}_{\boldsymbol{i}}+1$


Physical time $\downarrow$

## The Lamport Clock algorithm

1. Before executing an event $\mathbf{a}, C_{i} \leftarrow C_{i}+1$ :

- Set event time $C(\mathbf{a}) \leftarrow C_{i}$


Physical time $\downarrow$

## The Lamport Clock algorithm

1. Before executing an event $\mathrm{b}, \boldsymbol{C}_{\boldsymbol{i}} \leftarrow \boldsymbol{C}_{\boldsymbol{i}}+1$ :

- Set event time $C(b) \leftarrow C_{i}$


Physical time $\downarrow$

## The Lamport Clock algorithm

1. Before executing an event $\mathbf{b}, \boldsymbol{C}_{i} \leftarrow \boldsymbol{C}_{\boldsymbol{i}}+1$
2. Send the local clock in the message $m$


Physical time $\downarrow$

## The Lamport Clock algorithm

3. On process $\mathbf{P}_{\boldsymbol{j}}$ receiving a message $\mathbf{m}$ :

- Set $C_{j}$ and receive event time $C(\mathbf{c}) \leftarrow 1+\max \left\{C_{j}, C(\mathbf{m})\right\}$


Physical time $\downarrow$

## Ordering all events

- Break ties by appending the process number to each event:

1. Process $\mathbf{P}_{i}$ timestamps event $\mathbf{e}$ with $C_{i}(\mathbf{e}) . i$
2. $C(\mathbf{a}) . i<C(b) . j$ when:

- $C(\mathbf{a})<C(\mathbf{b})$, or $C(\mathbf{a})=C(\mathbf{b})$ and $i<j$
- Now, for any two events $\mathbf{a}$ and $\mathbf{b}, \mathrm{C}(\mathbf{a})<\mathrm{C}(\mathbf{b})$ or $\mathrm{C}(\mathbf{b})<\mathrm{C}(\mathbf{a})$
- This is called a total ordering of events


## Making concurrent updates consistent



- Recall multi-site database replication:
- San Francisco (P1) deposited \$100: \$
- New York (P2) paid 1\% interest: \%


## We reached an inconsistent state

Could we design a system that uses Lamport Clock total order to make multi-site updates consistent?

## Totally-Ordered Multicast

- Client sends update to one replica $\rightarrow$ Lamport timestamp C(x)
- Key idea: Place events into a local queue
- Sorted by increasing C(x)


Goal: All sites apply the updates in (the same) Lamport clock order

## Totally-Ordered Multicast (Almost correct)

1. On receiving an event from client, broadcast to others (including yourself)
2. On receiving an event from replica:
a) Add it to your local queue
b) Broadcast an acknowledgement message to every process (including yourself)
3. On receiving an acknowledgement:

- Mark corresponding event acknowledged in your queue

4. Remove and process events everyone has ack'ed from head of queue

## Totally-Ordered Multicast (Almost correct)

- P1 queues \$, P2 queues \%
- P1 queues and ack's \% - P1 marks \% fully ack'ed
- P2 marks \% fully ack'ed



## Totally-Ordered Multicast (Correct version)

1. On receiving an event from client, broadcast to others (including yourself)
2. On receiving or processing an event:
a) Add it to your local queue
b) Broadcast an acknowledgement message to every process (including yourself) only from head of queue $\checkmark$
3. When you receive an acknowledgement:

- Mark corresponding event acknowledged in your queue

4. Remove and process events everyone has ack'ed from head of queue

## Totally-Ordered Multicast ${ }^{\text {(Correct version) }}$



## So, are we done?

- Does totally-ordered multicast solve the problem of multi-site replication in general?
- Not by a long shot!

1. Our protocol assumed:

- No node failures
- No message loss
- No message corruption

2. All to all communication does not scale
3. Waits forever for message delays (performance?)

## Take-away points: Lamport clocks

- Can totally-order events in a distributed system: that's useful!
- But: while by construction, $\mathbf{a} \rightarrow \mathbf{b}$ implies $C(\mathbf{a})<C(\mathbf{b})$,
- The converse is not necessarily true:
- C(a) < C(b) does not imply a $\rightarrow \mathbf{b}$ (possibly, $\mathbf{a}|\mid \mathbf{b})$


# Can't use Lamport clock timestamps to infer 

 causal relationships between events
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## Vector clock (VC)

- Label each event $\mathbf{e}$ with a vector $V(\mathbf{e})=\left[c_{1}, c_{2} \ldots, c_{n}\right]$
$-c_{i}$ is a count of events in process $i$ that causally precede $\mathbf{e}$
- Initially, all vectors are $[0,0, \ldots, 0]$
- Two update rules:

1. For each local event on process $i$, increment local entry $c_{i}$
2. If process $j$ receives message with vector $\left[d_{1}, d_{2}, \ldots, d_{n}\right]$ :

- Set each local entry $c_{k}=\max \left\{c_{k}, d_{k}\right\}$
- Increment local entry $c_{j}$


## Vector clock: Example

- All counters start at [0, 0, 0]
- Applying local update rule
- Applying message rule
- Local vector clock piggybacks on interprocess messages



## Vector clocks can establish causality

- Rule for comparing vector clocks:
$-\mathrm{V}(\mathrm{a})=\mathrm{V}(\mathrm{b})$ when $\mathbf{a}_{k}=\mathbf{b}_{k}$ for all $k$
$-\mathrm{V}(\mathrm{a})<\mathrm{V}(\mathrm{b})$ when $\mathbf{a}_{k} \leq \mathbf{b}_{k}$ for all $k$ and $\mathrm{V}(\mathbf{a}) \neq \mathrm{V}(\mathrm{b})$
- Concurrency: $\boldsymbol{a} \| \boldsymbol{b}$ if $\mathbf{a}_{i}<\mathbf{b}_{i}$ and $\mathbf{a}_{j}>\mathbf{b}_{j}$, some $i, j$
- $\mathrm{V}(\mathrm{a})<\mathrm{V}(\mathrm{z})$ when there is a chain of events linked by $\rightarrow$ between a and $z$



## Two events a, z

## Lamport clocks: C(a) < C(z) Conclusion: None

Vector clocks: $\mathrm{V}(\mathrm{a})<\mathrm{V}(\mathrm{z})$
Conclusion: a $\rightarrow \ldots \rightarrow$ z

## Vector clock timestamps tell us about causal event relationships

# VC application: <br> Causally-ordered bulletin board system 

- Distributed bulletin board application
- Each post $\rightarrow$ multicast of the post to all other users
- Want: No user to see a reply before the corresponding original message post
- Deliver message only after all messages that causally precede it have been delivered
- Otherwise, the user would see a reply to a message they could not find


## VC application: Causally-ordered bulletin board system



- User 0 posts, user 1 replies to 0's post; user 2 observes


# Wednesday Topic: Lab 1 - Virtualization, sockets, RPCs 

## Why global timing?

- Suppose there were an infinitely-precise and globally consistent time standard
- That would be very handy. For example:

1. Who got last seat on airplane?
2. Mobile cloud gaming: Which was first, A shoots B or vice-versa?

3. Does this file need to be recompiled?

## Totally-Ordered Multicast ${ }^{(\text {Attempt\#1) }}$

- P1 queues \$, P2 queues \%
- P1 queues and ack's \%
- P1 marks \% fully ack'ed
- P2 marks \% fully ack'ed
- P2 processes \%
- P2 queues and ack's \$
- P2 processes \$
- P1 marks \$ fully ack'ed
- P1 processes \$, then \%



## Totally-Ordered Multicast (Correct version)

- P1 queues \$, P2 queues \%
- P1 queues \%
- P2 queues and ack's \$
- P2 marks \$ fully ack'ed
- P2 processes \$
- P1 marks \$ fully ack'ed
- P1 processes \$
- P1 ack's \%
- P1 marks \% fully ack’ed
- P1 processes \%
- P2 marks \% fully ack'ed
- P2 processes \%



## Time standards

- Universal Time (UT1)
- In concept, based on astronomical observation of the sun at $0^{\circ}$ longitude
- Known as "Greenwich Mean Time"
- International Atomic Time (TAI)
- Beginning of TAI is midnight on January 1, 1958
- Each second is $9,192,631,770$ cycles of radiation emitted by a Cesium atom
- Has diverged from UT1 due to slowing of earth's rotation
- Coordinated Universal Time (UTC)
- TAI + leap seconds, to be within 0.9 seconds of UT1
- Currently TAI - UTC = 36


## VC application: Order processing

- Suppose we are running a distributed order processing system
- Each process = a different user
- Each event = an order
- A user has seen all orders with V (order) < the user's current vector

